

# monet-3

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# Scaling Up in Size and Knowledge

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- **The Good News:**

QSIM predicts all possible behaviors consistent with given qualitative and semi-quantitative knowledge.

- **The Bad News:**

QSIM output can be large, even infinite.

The problem is real, not spurious, behaviors.

- **The Good News:**

There are solutions.

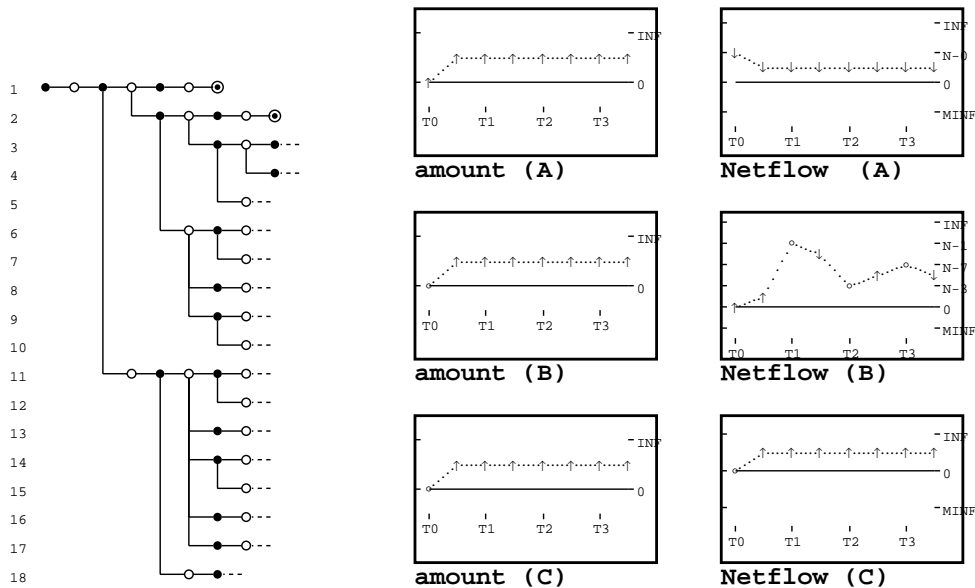
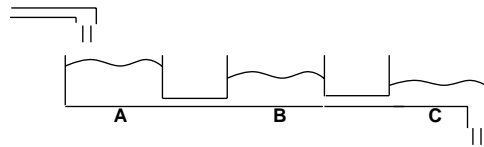
# Four Solutions to Intractability

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- **(1) Chatter Abstraction:** detect and abstract a region of unconstrained change to a single qualitative state.
- **(2) Model Decomposition:** use both state-based and history-based simulation to ignore irrelevant relationships.
- **(3) Temporal Logic Model-Checking:** use a theorem-prover to query the behavior tree.
- **(4) Temporal Constraints:** guide the simulator's attention to specified portions of the state space.

# (1) The Problem of Chatter

Chatter occurs when a variable's direction of change is unconstrained, except by continuity.

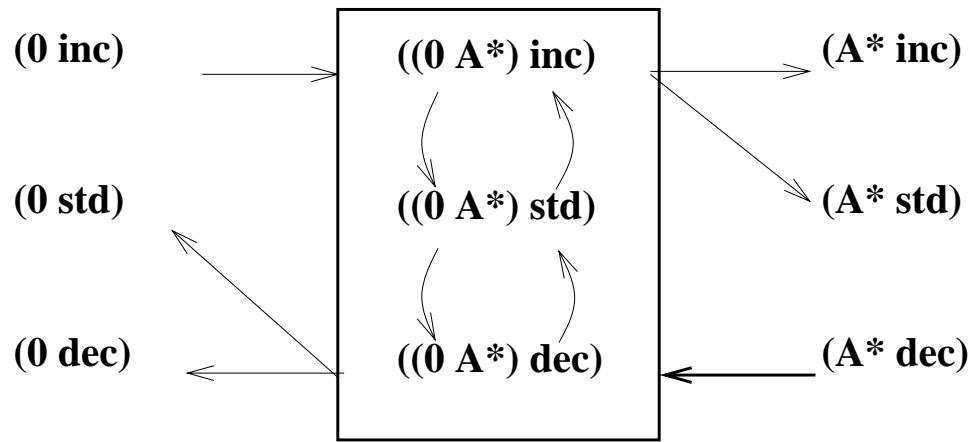


Chatter in one variable can propagate to others.

# The Chatter Box

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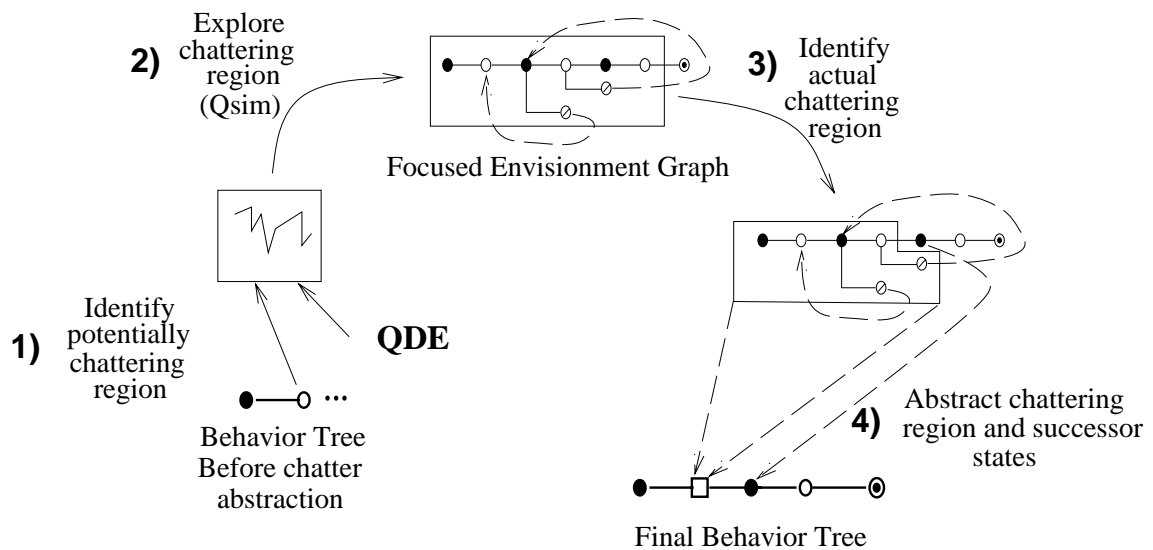
Qualitative behaviors are trajectories through state space.  
Chatter is a property of a region of the state space.



Sometimes knowledge of higher-order derivatives can help.  
Often not.

# Chatter Box Abstraction

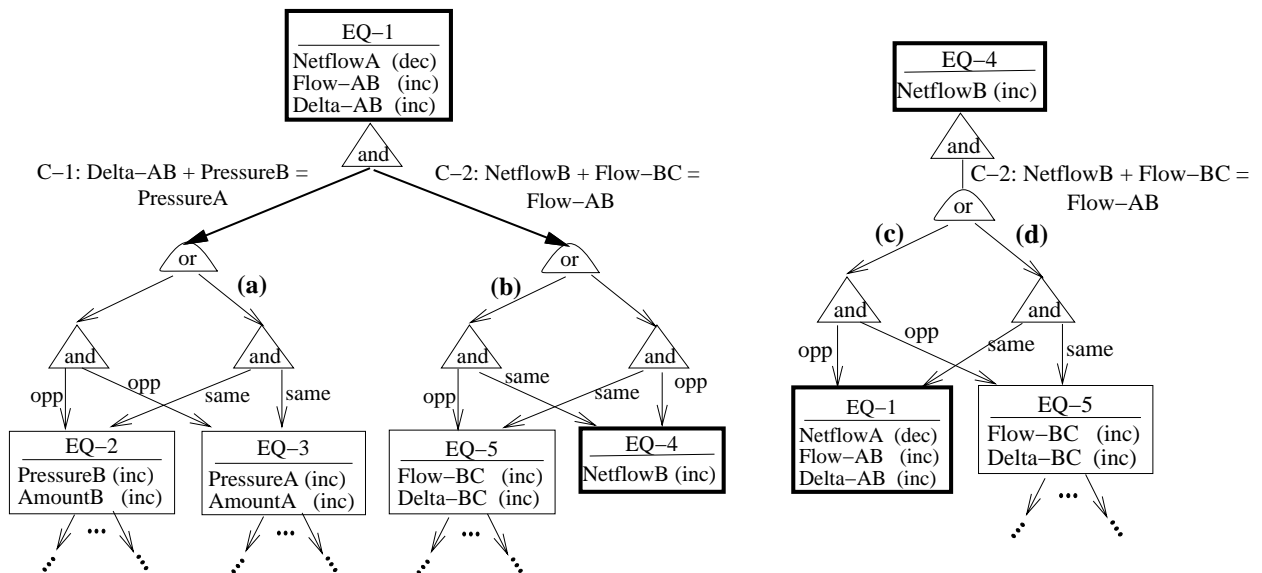
- Detect entry into a chatter box.
- Identify chattering variables and boundary values.
- Do focused envisionment to detect exits from chatter box.
- Replace envisionment with a single abstract state.



But: envisionment is still exponential in number of chattering variables.

# Dynamic Chatter Abstraction

- Detect entry into chatter box.
- Create *chatter dependency graph*:



- Evaluate status of classes of chatter-equivalent variables.
- Simulate with abstracted qdirs. (Unique values indicate exit from chatter box.)

Analysis is complex, but the algorithm is efficient.

## (2) Model Decomposition

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- **The Problem:**

- Basic QSIM uses a global state representation.
- Unrelated changes must be temporally ordered.
- Branch on all possible orders.

- **The Solution:**

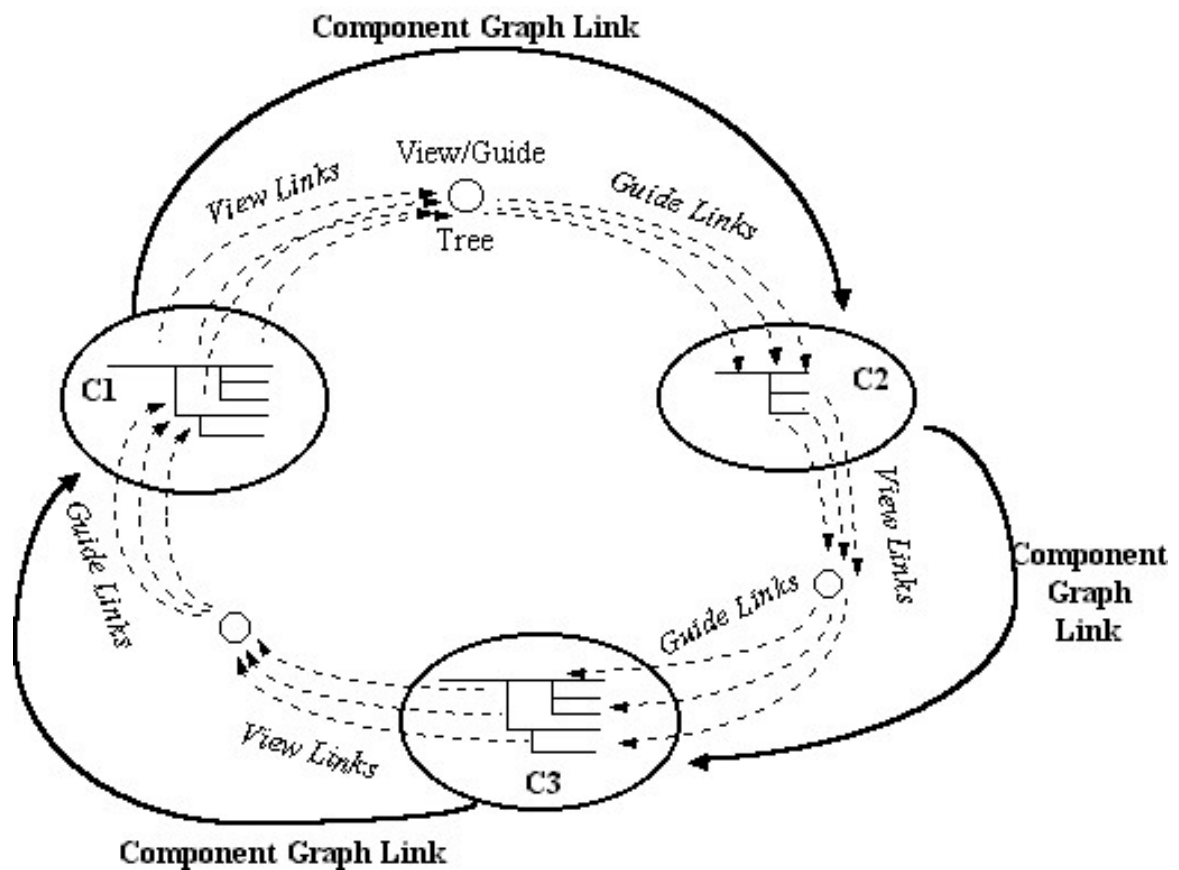
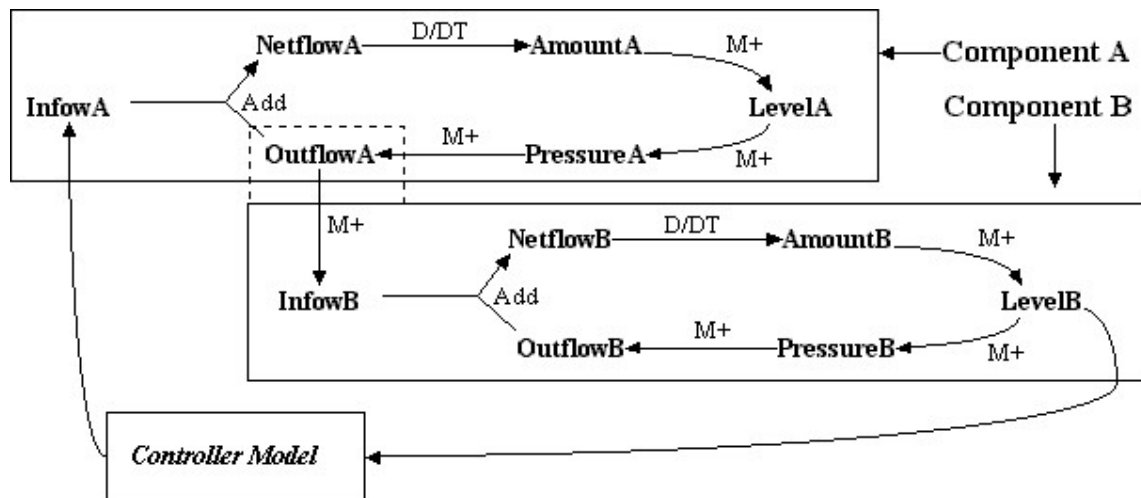
- Decompose complex model into weakly-interacting components. [Simon, 1969]
- Combine component behaviors into model behavior.

# QSIM = Temporally-Extended CSP

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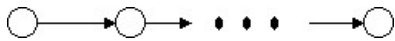
- Compute *all* behaviors of each component.
  - State-based simulation within components.
  - Abstract values for unknown boundary variables.
  - Guided simulation for known boundary variable behavior.
- Each component behavior must belong to *some* global behavior.
  - History-based analysis between components.
  - Causal dependency among components controls simulation order: sequential or concurrent.
- Record dependencies among component behaviors.

# Example: Controlled Two-Tank Cascade



# Efficiency Gains on N-Tank Systems

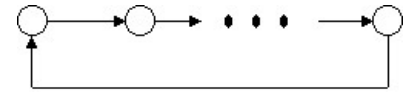
Different causal topologies:



**Cascade**

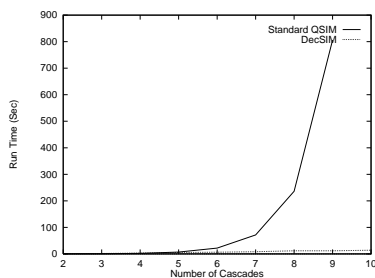


**Chain**

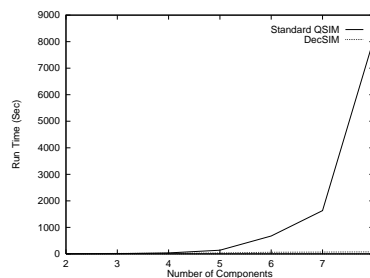


**Loop**

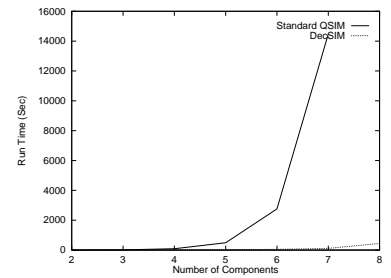
Number of Comp's	Cascade		Chain		Loop	
	QSIM	DecSIM	QSIM	DecSIM	QSIM	DecSIM
2	0.204	0.815	3.075	6.79	0.757	5.587
3	0.621	1.6	10.94	19.903	16.149	8.147
4	2.2	3.12	37.55	25.984	89.418	12.67
5	7.09	5.49	139.3	36.712	493.88	23.28
6	21.92	6.32	676	62.405	2758	48.73
7	71.59	8.39	1633	70	14474	116.1
8	236	11.67	8101	77	nc	442.4
9	806	11.75	nt	nt	nt	nt
10	nc	14.05	nt	nt	nt	nt



**Cascade**



**Chain**



**Loop**

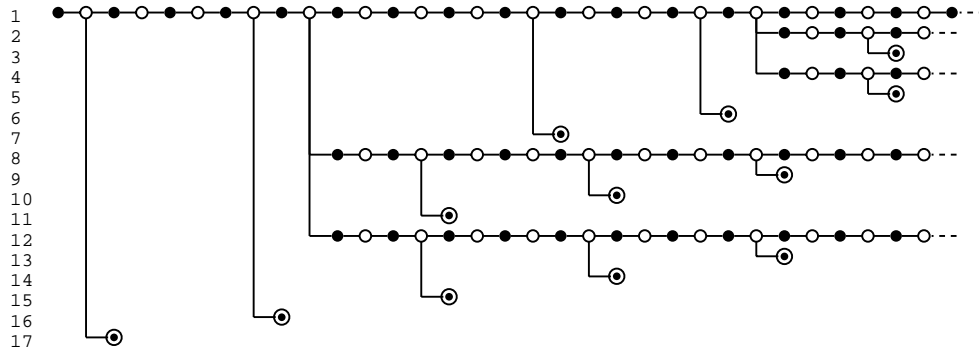
### (3) Temporal Logic Model-Checking

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- Temporal logic expresses what we want to know about the behaviors.
- The QSIM behavior tree can be viewed as a model for statements in a branching-time temporal logic.
- Model-checking determines whether a statement is true of the behavior tree.
  - Sound and complete.
- QSIM behavior tree predicts behaviors of dynamical systems.
  - Guaranteed coverage, but possible spurious behaviors.  
(Filtering is sound but incomplete.)

A universal statement can thus be proved by qualitative simulation.

# Temporal Logic and Behavior Trees



modal	temporal	logical	QSIM
<i>necessarily</i>	<i>until</i>	<i>and</i>	<i>qval</i>
<i>possibly</i>	<i>next</i>	<i>or</i>	<i>status</i>
	<i>eventually</i>	<i>implies</i>	<i>funcall</i>
	<i>always</i>	<i>not</i>	

Simulating KJA PI controller.

Behavior tree rooted at S-0,

with 1 initial states and 17 behaviors.

Some behaviors don't terminate...

Checking: (EVENTUALLY (STATUS QUIESCENT)).

Validity = (NIL NIL T NIL T T T NIL T T T NIL T T T T T).

...but all that terminate have zero error.

Checking: (NECESSARILY (ALWAYS (IMPLIES (STATUS QUIESCENT)  
(QVAL E (0 STD))))).

Validity = T.

Every fixed point is stable.

Checking: (NECESSARILY (ALWAYS (IMPLIES (STATUS QUIESCENT)  
(STATUS STABLE))))).

Validity = T.

## Technical Issues

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Matching assumptions between QSIM and Model-Checking.

- A behavior tree is *closed* when every behavior terminates with a quiescent state, a region transition, or a cycle.
- The QSIM Guaranteed Coverage theorem applies only to closed behavior trees.
- For effective model-checking, cycles in the behavior tree output by QSIM must be unwound one extra time.

# The Main Theorem

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- **Main Theorem:**

- If  $\Phi$  is a universal state formula in EBTL and  $M$  is a closed tree and  $(TL\ M\ \Phi)$  returns T, then  $\Phi'$  is true of every real function consistent with the QDE.

- **Lemma:** the QSIM Guaranteed Coverage Theorem

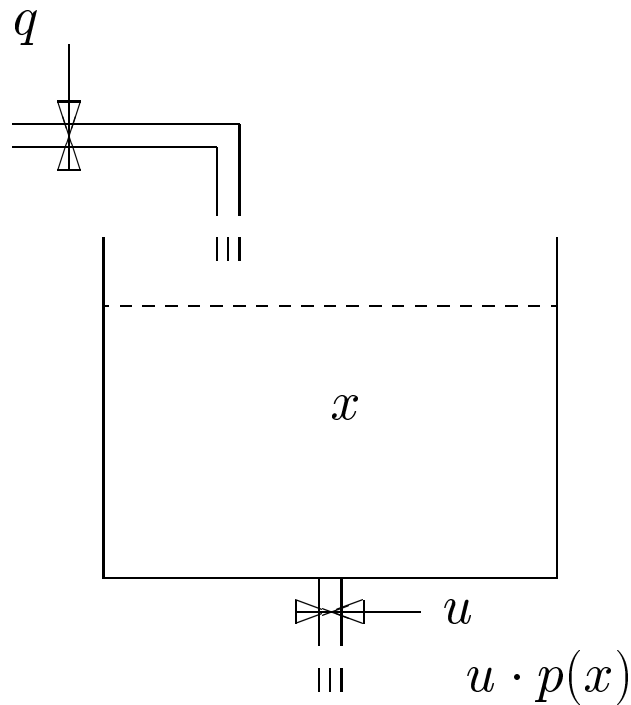
- If QSIM returns a closed tree then QSIM predicts every real function consistent with the QDE input.

- **Caveats:**

- If  $M$  is not closed, some real behaviors may not be predicted (yet).
- If  $\Phi$  is not universal, the model of  $\Phi'$  could be a spurious behavior.

# Level Control of the Water Tank

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$$\dot{x} = f(x, u) = q - u \cdot p(x).$$

$x$  = amount in tank

$q$  = inflow into tank

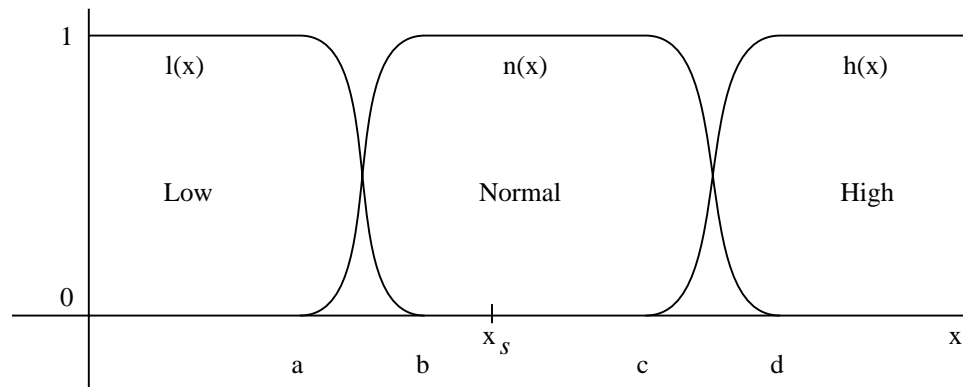
$u$  = drain area

$p(x)$  = influence of pressure at drain

# A Heterogeneous Controller

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**The operating regions and their appropriateness measures:**



**The local control laws:**

$$x \in Low \Rightarrow u_l(x) = 0$$

$$x \in Normal \Rightarrow u_n(x) = k(x - x_s) + u_s$$

$$x \in High \Rightarrow u_h(x) = u_{max}$$

**The global control law:**

$$u(x) = l(x)u_l(x) + n(x)u_n(x) + h(x)u_h(x).$$

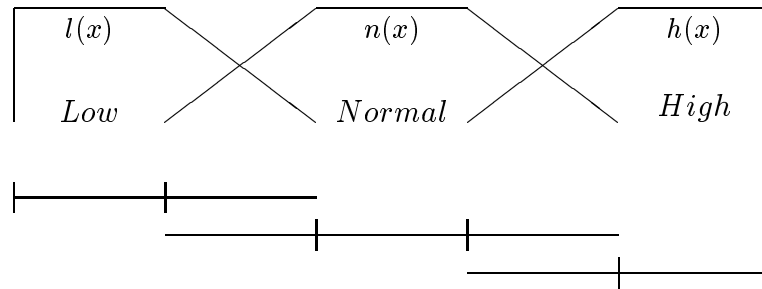
**The discrete abstraction:**



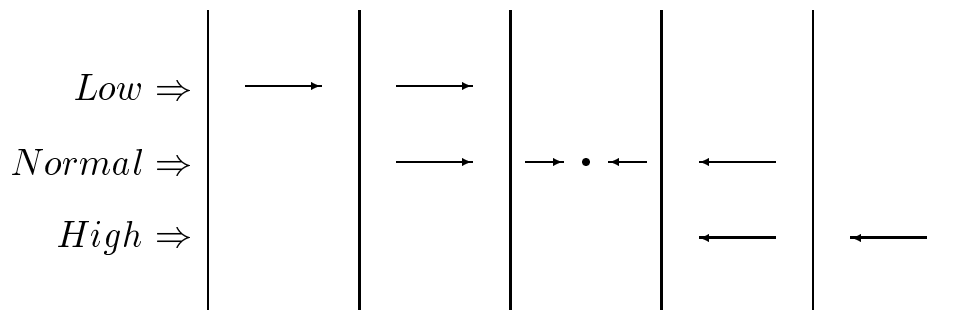
# Qualitative Combination of Behaviors

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- Overlapping operating regions for the local laws.



- Require qualitative agreement where laws overlap.



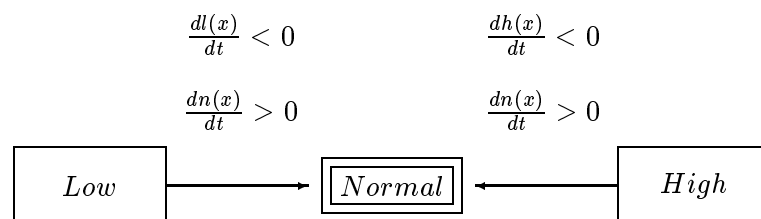
- Guarantee monotonic behavior in overlap regions.

$$Low \Rightarrow q > 0$$

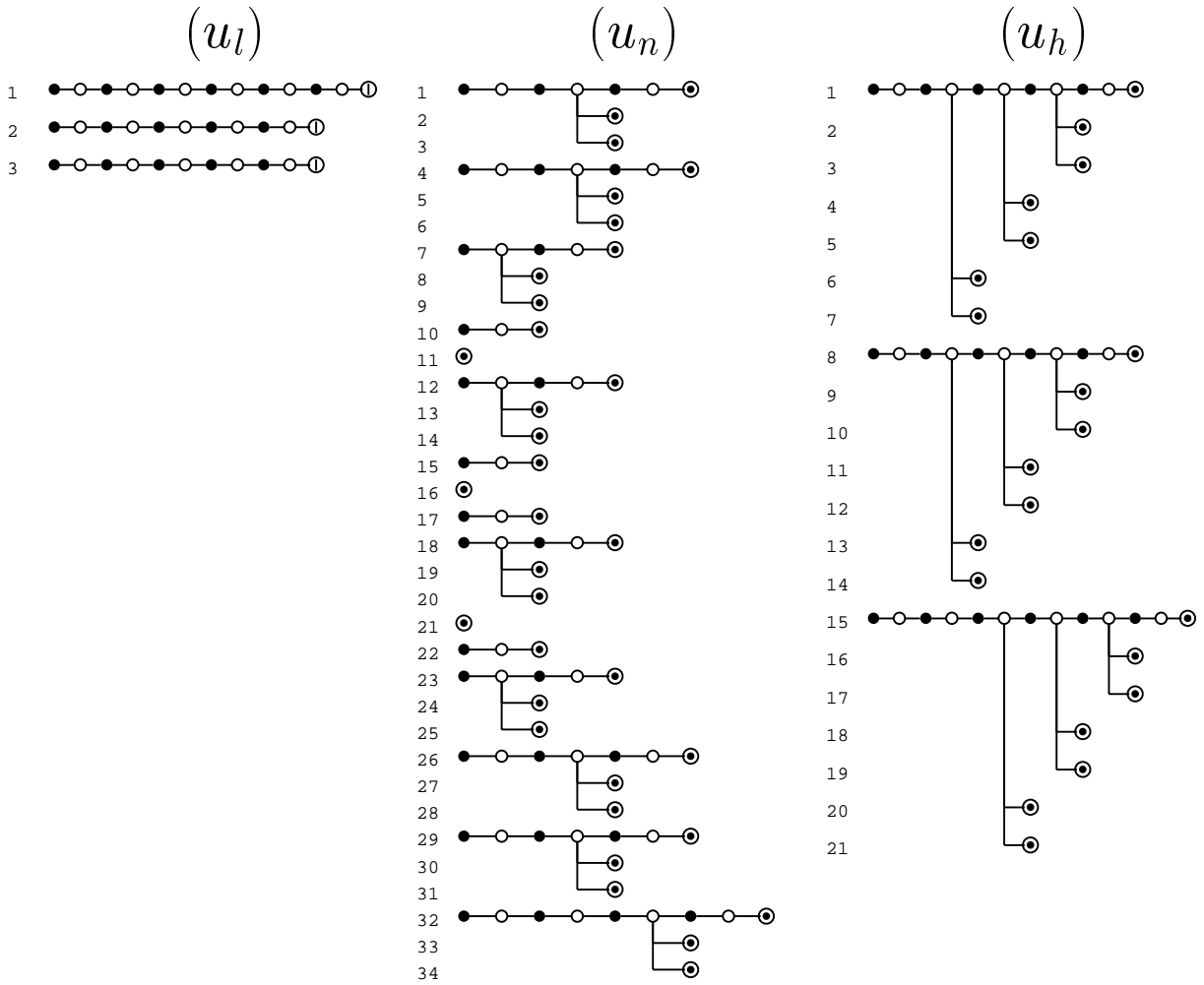
$$Normal \Rightarrow q_b < q < q_c$$

$$High \Rightarrow q < u_{max} \cdot p(c)$$

- Abstract the control law to a finite transition diagram.



# Behavior Trees for Local Control Laws



# Validity of Qualitative Properties

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Simulating controller U<sub>l</sub>.

Behavior tree rooted at S-0, with 3 initial states and 3 behaviors.

Checking UPWARD-MOTION: (NECESSARILY (ALWAYS (IMPLIES (QVAL X ((NIL B) NIL  
(QVAL X (NIL INC))))))

Validity at S-0 = T.

Checking DESTINATION: (NECESSARILY (EVENTUALLY (QVAL X ((B C) NIL)))).

Validity at S-0 = T.

Simulating controller U<sub>n</sub>.

Behavior tree rooted at S-40, with 16 initial states and 34 behaviors.

Checking UPWARD-MOTION: (NECESSARILY (ALWAYS (IMPLIES (QVAL X ((NIL B) NIL  
(QVAL X (NIL INC))))))

Validity at S-40 = T.

Checking DOWNWARD-MOTION: (NECESSARILY (ALWAYS (IMPLIES (QVAL X ((C NIL) NIL  
(QVAL X (NIL DEC))))))

Validity at S-40 = T.

Checking DESTINATION: (NECESSARILY (EVENTUALLY (QVAL X ((B C) NIL)))).

Validity at S-40 = T.

Checking STABILITY: (NECESSARILY (EVENTUALLY (AND (QVAL X ((B C) STD))  
(STATUS QUIESCENT)  
(STATUS STABLE)))).

Validity at S-40 = T.

Simulating controller U<sub>h</sub>.

Behavior tree rooted at S-167, with 3 initial states and 21 behaviors.

Checking DOWNWARD-MOTION: (NECESSARILY (ALWAYS (IMPLIES (QVAL X ((C NIL) NIL  
(QVAL X (NIL DEC))))))

Validity at S-167 = T.

Checking DESTINATION: (NECESSARILY (EVENTUALLY (QVAL X ((B C) NIL)))).

Validity at S-167 = T.

## (4) Temporal Constraints: TeQSIM

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Temporal logic lets the modeler use knowledge not expressible in the QDE or SQDE.

- Trajectory constraints describe intended behaviors.
  - Time-varying exogenous variables.
  - Events and discontinuous changes.
  - Semi-quantitative bounds on behaviors.
- Interleave QSIM with the temporal logic model-checker.  
Accept only behaviors consistent with TL constraints.
- Focus attention on subset of behavior space.

# TeQSIM Examples

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- Specify exogenous input.

```
(event step-up :time (2 3))
(event step-down :time (17 24))
(disc-change (event step-up)
              ((inflow (normal high)
                       :range (1500 1800)))
              (event step-down)
              ((inflow normal)))
```

- Focus on overflow scenario.

```
(event open)
(disc-change (event open)
              ((valve (normal max)
                       :range (4 nil))))
(before (qvalue level (top nil)) (event open))
(eventually (qvalue level (top nil)))
```

Derive temporal bounds on (event open) to prevent overflow.

## More Information:

<http://www.cs.utexas.edu/users/qr>

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### Qualitative Reasoning

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- Daniel J. Clancy and Benjamin Kuipers. 1997. Static and dynamic abstraction solves the problem of chatter in qualitative simulation. *AAAI-97*.
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- Benjamin Shults and Benjamin Kuipers. 1997. Proving properties of continuous systems: qualitative simulation and temporal logic. *Artificial Intelligence Journal* **92**: 91–129.
- Benjamin J. Kuipers and Karl J. Åström. 1994. The composition and validation of heterogeneous control laws. *Automatica* **30**(2), February 1994.