Qualitative physics as a component in natural language semantics: A progress report

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Abstract

We propose that qualitative physics can provide an important component of natural language semantics. Specifically, we describe how qualitative process theory can be recast in terms of frame semantics, as used in the Berkeley FrameNet project. This reformulation is important because it could allow the techniques of qualitative reasoning to be harnessed for natural language understanding and it expands the range of phenomena that can be described in NL semantics. We show that these ideas can account for a large percentage of a small corpus of explanatory text, and that they support the construction of QP models from such texts.

Introduction

Understanding the semantics of natural language is a central problem in cognitive science. Such an understanding must connect fundamentals of our conceptual structure to their realizations in linguistic forms, and thus must draw upon both insights about language and about conceptual structure. Significant progress is being made on the language side, with projects such as FrameNet (Fillmore et al 2001) developing broad systems that capture aspects of the meaning of words and linguistic constructions in terms of frame semantics (Fillmore & Atkins, 1994). Significant progress is also being made on understanding aspects of human conceptual structure, for example, the work carried out in the qualitative reasoning community. Qualitative reasoning focuses on the representations necessary to reason about the physical world, ranging from everyday phenomena to the work of scientists and engineers. While many QR efforts are aimed at applications, some efforts are aimed directly at modeling human reasoning about physical systems (cf. Bredeweg & Schut, 1991; Kuipers & Kassirer 1984; Kuipers et al 1988; Forbus & Gentner 1986, 1997). Ultimately these two lines of investigation, natural language semantics and the understanding of human conceptual structures, need to join forces. In the words of the FrameNet team¹: "In the end it will be necessary to express frame notions in some formal knowledge-representation language which will allow valid inferences to be drawn from frame semantic representations of sentences, or which

This paper is a first step in linking these investigations. We propose that qualitative process theory (Forbus 1984) can provide such a knowledge representation language for aspects of frame semantics concerned with continuous parameters and continuous causation. QP theory concerns the structure of a class of physical theories, and has been successfully used in a variety of reasoning systems (Forbus, 1996). The hypothesis is that many mental models of physical phenomena can be expressed in this formalism. QP theory has been used to develop a wide range of models of phenomena, including economic and medical models in addition to physical models. This makes it an excellent candidate for a component in a larger system of natural language semantics.

We begin by building a theoretical bridge between QP theory and frame semantics, as exemplified in FrameNet. We briefly review the relevant aspects of QP theory and show how they can be recast in terms of frame semantics. This recasting provides a means for defining frames for physical processes and relationships involving continuous parameters. We illustrate how these ideas can be used to extend a natural language semantics by an analysis of flow.

With the theoretical bridge in place, we provide empirical support for it via a corpus analysis of an explanatory text. This analysis provides evidence concerning two questions. First, we explore how much of the explanation these frames can account for. Second, we analyze whether a qualitative model can be reconstructed from the text using these frames. Finally, we discuss some new issues raised by this approach and plans for future work.

Qualitative physics in frame semantics

We begin by recasting QP theory in terms of frame semantics, as used in FrameNet. We review the ontological assumptions underlying QP theory and their implications for the organization of the frame system. Next we discuss physical processes and their occurrences, followed by an analysis of how qualitative mathematics is expressed. We conclude this section by showing that this analysis is compatible with analyses of overlapping phenomena already in FrameNet.

can serve in a precise way in the development of a cumulative representation of the content of an ongoing discourse."

¹ The FrameNet project's home is the International Computer Science Institute in Berkeley, CA. A detailed description of the project can be found at http://www.icsi.berkeley.edu/~framenet

Ontological assumptions

In QP theory, physical changes in continuous properties are caused by physical processes. Examples of physical processes include kinds of flows (e.g., heat, liquid, gas), phase changes (boiling, freezing), and some aspects of motion. Ontologically, physical processes serve as the mechanisms of physical causality: All naturally occurring changes (and many of the indirect effects of the actions of agents) are ultimately caused by the activity of one or more physical processes. Instances of physical processes exist when an appropriate configuration of participants occurs. Such process instances are active over any span of time for which their conditions hold. When a process instance is active, its consequences hold. For example, two thermal entities (i.e., having the continuous property heat) that are thermally in contact give rise to two instances of heat flow, one in each potential direction. Whether or not either of these is active depends in turn on the relative temperatures between the two bodies.

The consequences of a physical process are of three types. First, there are *direct influences* that represent the direct effects that a physical process has on the world. For example, heat flow causes the heat of the source of the flow to decrease while increasing the heat of the destination. Second, there are other dynamical properties defined, including new parameters and causal laws, which describe how changes propagate through continuous properties. For example, the rate at which heat flows is a continuous property, and it is determined by the difference between the temperatures. Third, other properties that hold while the process is occurring, such as appearance information, can be consequences. In everyday boiling, for instance, one typically sees bubbles.

Two key conceptual advances in qualitative modeling are the insights that (1) many important kinds of reasoning about dynamical systems can be done without numerical information or mathematical models and (2) qualitative relationships can be formulated which explicitly capture patterns of human causal reasoning. These causal connectives are summarized below; see (Forbus 1984) for details. The values of continuous parameters tend to be expressed in comparative terms, via ordinal relationships constraining a parameter with respect to other relevant properties. If an object participates in process instances of heat flow, for example, then its temperature is defined in terms of its relationships with the temperatures of the other objects participating in those heat flows.

This summary highlights three important properties of QP theory that makes it potentially a valuable component of natural language semantics. First, the notion of physical process it defines is psychologically plausible. Descriptions of physical processes are abundant in language concerning physical phenomena, and are routinely used in metaphors (cf. Lakeoff 1980, Gentner et al 2001). Second, the causal account QP theory provides is consistent with human causal explanations in most physical domains (Forbus & Gentner 1986, 1997). Third, the abstract level of information that

qualitative representations support seems a natural fit for the level of specificity commonly found in natural language descriptions of physical principles and situations. One does not need to understand differential equations or carry out detailed simulations to understand physical metaphors ("her anger mounted until she boiled over").

Recall that in frame semantics, meaning is expressed in terms of systems of structured representations, frames, whose parts (called frame elements, abbreviated FE) are bound to parts of a text and have associated with them inferences that provide meaning (Fillmore & Atkins, 1994). The packaging of physical knowledge and principles in QP theory (inspired in part by Minsky's (1975) notion of frames) suggests a natural alignment with frame semantics. There is a basic physical process frame, whose structure provides the fundamental aspects of physical processes. Subframes describe particular categories of physical processes, with differences in their participants and consequences being the differentia that set them apart. Instances of these frames are combined with frames from other aspects of the semantics to create the frame system describing the meaning of a text. The qualitative causal mathematics of QP theory is expressed through another collection of frames. In addition to their role in physical process descriptions, these qualitative causal frames can be used for other domains with continuous parameters, such as economics or metaphorical extensions of physical concepts. The next three subsections outline these frame systems.

Processes and their occurrences

The Physical Process frame involves four types of FEs:

- Participant specifies one of the participants in the physical process. Example: in "Heat flows from the hot brick to the cool room", "hot brick" and "cool room" are Participants in an instance of the HeatFlow frame.
- Condition specifies one of the conditions under which the process is active. Example: in "Heat flows from one place to another because the temperature of the two places is different." the condition is the difference in temperature values (see ordinals below)
- Status specifies whether or not the process is active. Example: In "The radiator leak was stemmed by shoving a cloth into it." The word stemmed suggests that a flow which was enabled is now stopped. We say that the status is active when the process is occurring, and inactive otherwise.
- Consequence specifies one of the direct consequences of the physical process. Example: In "Water flooded into the room when the valve broke." the liquid flow into the room has as one of its Consequences an increase in the amount of water in the room.

These frame elements can be directly mapped to the formal models that QP theory supports. For a process type or instance, the set of participants collectively define the collections of entities it occurs among. The union of the conditions is the set of conjuncts that comprise the necessary and sufficient conditions for it to be active. The

set of fillers for the consequences FEs constitute its direct consequences.

Our analysis of the syntactic realizations of these frame elements, and the others reported here, is work in progress, and we plan to analyze a much larger corpus to ensure that our results are robust. That, plus space limitations, will limit our discussion of syntactic realizations to a few stable highlights. Noun phrases that serve as the primary actor and object in a sentence tend to be participants, e.g., in "A hot brick loses heat to a cool room." "Hot brick" and "cool room" are participants. Certain frame elements already used in other FrameNet frames, e.g., Source and Destination, tend to be participants when a physical process is the actor. The patterns that indicate conditions include "condition causes Process", "Process occurs when Condition.", and "Process depends on Condition." For consequences, there are two cases: influences and other consequences. Influences are discussed below. The other consequences, since they can range over almost any physical statement in principle (e.g., appearances, sounds, etc.), are difficult to characterize concisely. Example indicators are occurrences of the FrameNet FEs of Manner and Result.

Parameters and values

Continuous properties are represented by the Quantity frame, which has the following elements:

- Entity specifies what this property is a property of. Typically this is unique. Example: "brick" in "the temperature of the brick"
- *QuantityType* specifies the kind of parameter that this is. Example: "temperature" in "temperature of the brick."
- *Value* specifies the numerical value of the property. This FE is optional. Example: "3" in "3 liters of water".
- *Units* specifies the physical units of the property. This FE is optional. Example: "kilograms" in "3 kilograms of lead".

Ds specifies how the parameter is changing and stands for "sign of the derivative". This FE is optional. Example: In "The temperature is increasing." the sign is expressed by the word "increasing" which would be mapped to the value of 1. While syntactic realizations for quantity types, values and units are fairly obvious, DS manifests itself in the text many different ways, e.g. -1 could show up as "falling", "decreasing", etc.

Values and units are often not explicitly stated or even filled in via default, but Ds and comparative statements about values are common. These are expressed via the Ordinal frame, which has the following FEs:

- Q1, Q2 specify the quantities being compared. Either is optional. Example: "the coffee's temperature".
- OrdReln specifies the relationship between the values of the quantities. It must be one of <, >, =, \ge , \le , =, \ne , sameorder, or negligible. Example: In "Evaporation can be ignored" the word "ignored" refers to a negligible OrdReln of the rate of an evaporation process compared to other processes being described.

Ordinal relations provide a useful qualitative notion of value because they often serve as conditions for physical processes and states (e.g., flows occur when a driving parameter is unequal, equilibriums occur when opposing effects are equal). Syntactic realizations of ordinals are usually described via explicit comparisons (e.g., "Q1 is greater than Q2") or as some type of comparative construction. One very common pattern is the use of ordered dimensional adjectives to set up a tacit comparison. For instance, from "hot brick" and "cool room", one knows an ordinal relationship involving their temperature due to the meanings of "hot" and "cool".

Qualitative mathematics and causality

The causal relationships between quantities are expressed via a qualitative mathematics that supports partial information about the nature of the connections between them. The basic frame is the Influence, whose FEs are

- Constrained specifies the dependent quantity, i.e., the effect.
- *Constrainer* specifies the independent quantity, i.e., a proximal cause for the constrained quantity.
- Sign specifies the direction, which can be + or -. It is expressed by words such as "up", "down", "greater", "more", "less" etc.

There are two subframes of the Influence frame, DirectInfluence and Qprop. These correspond to the QP theory primitives I+/I- and $\propto_{Q+}/\propto_{Q-}$ respectively (Forbus 1984). While the two subframes share frame elements, the underlying semantics is quite different. For direct influences, the constrainer is combined via addition to other constrainers to determine (qualitatively) the derivative of the constrained quantity, and the sign indicates whether it is a positive or negative contribution to that sum. For Qprop, the Constrained is functionally dependent on the Constrainer, and perhaps on other properties as well, with the sign indicating whether the dependence is increasing or decreasing monotonic. This is the weakest distinction that enables changes to be propagated through causal laws.

As their common heritage suggests, in some cases the syntactic realizations of these two kinds of influences can be quite close. However, many cases are straightforward. Some realizations for <code>Qprop</code> include "Constrained **depends on** Constrainer." and "**As** Constrainer Ds, Constrained Ds." For example, "As the air temperature goes up, the relative humidity goes down" is clearly a <code>Qprop</code>, with <code>Constrained</code> = "relative humidity", <code>Constrainer</code> = "air temperature", and <code>sign</code> = -.

Syntactic realizations for DirectInfluences are more complex. In advanced texts one can find patterns such as "The rate of Constrained depends on Constrainer." but they do not seem common. In everyday texts explicit discussions of rates seem even rarer. Instead, DirectInfluences tend to occur in larger-scale patterns, often tied to a generalized notion of motion. For example, "Most water in the air comes from evaporation." is a

DirectInfluence, with Constrained = "water in the air",
Constrainer = "[rate of] evaporation" and sign = +. 2

Compatibility with existing frame semantics

One implication for semantics is that, in addition to the frames associated with QP theory per se, there will be a collection of subframes corresponding to particular kinds of physical phenomena, such as flows, motion, and phase changes. And indeed FrameNet already has an existing analysis of motion that is compatible with OP theory. The FEs of Theme, Source, Goal, and Path are finer-grained distinctions of the FE Participant in the general PhysicalProcess frame. In QP theory models of this kind of motion (cf. Forbus 1984), there is a quantity Position that is referenced to the Path from Source to Goal. A DirectInfluence frame with Constrained = Position and Constrainer = Velocity is a Consequence of the Motion frame. An ordinal frame with Q1 = velocity, Q2 = zero, and $OrdReln = \neq is$ the Condition for the Motion frame. This compatibility is encouraging, since it means that the implications that can be drawn from qualitative reasoning could be made available in service of natural language understanding.

Example: An analysis of flow

Next we present an analysis of an important frame for physical phenomena, flow. We start with well-worked out ideas in the qualitative physics literature, using the framework above to recast them into frame semantics. This frame is used in our corpus analysis below.

The general Flow frame

The model of flow we are starting with is based on those in Forbus (1984). Several of the frame elements are specializations of Participant:

- FlowSource specifies the starting region of the flow.
- FlowDest specifies the region where what is flowing ends up.
- FlowPath specifies the path along which the flow occurs

These FEs determine the overall type of flow occurring:

- FlowDriver specifies the intensive quantity (e.g., something like pressure or temperature) whose difference at source and destination drives the flow.
- FlowQ specifies the extensive quantity (e.g., something like mass or heat) that is directly influenced by the flow. Optional.
- FlowStuff specifies the "stuff" which is considered to be flowing. Optional.

Typically texts mention either FlowQ or FlowStuff but not both. Many uses of the Flow frame are metaphorical from a

² Note that 'from evaporation' refers to an internal quantity of a process (i.e. the evaporation rate), not to a participant (as in 'from the ocean'). The latter would be marked as a source, not as a constrainer.

scientific perspective (e.g., heat is not a substance), but may be literal from a common sense perspective, depending on the language user's mental models. FlowStuff must be continuous in nature (hence FlowQ must exist, even if not explicitly mentioned) for the idea of flow to make sense.

There are two condition FEs for Flow. The first is an Ordinal, i.e., that the FlowQ(FlowSource(Flow)) is greater than FlowQ(FlowDest(Flow)). The second is that FlowPath not be blocked. The nature of being blocked depends on the subframe of Flow. For instance, a stopper can block liquid flow, but heat can still pass.

Flow has three Consequence FEs: a Quantity whose QuantityType is Rate, and two DirectInfluence frames, constraining the FlowQ of FlowSource and FlowDest via Rate(Flow) with the appropriate signs.

More sophisticated versions of this basic pattern are common in qualitative modeling; e.g., the rate is typically a function of the difference between the driving quantities, and also depends on path properties. Such elaborations do commonly appear in explanatory texts, and consequently the ability of qualitative modeling to support such incremental elaboration, which can be done via additional Qprop frames in this case, provides a necessary source of representational flexibility for natural language semantics.

Some empirical evidence

Up to now we have been concerned with expressing the concepts of QP theory in Frame Semantics, showing how they can fit into this larger system and some of their syntactic realizations in English. Here we examine the utility of doing this, in two ways. First, we turn the question around: How much do these ideas contribute to understanding the semantics of texts involving the physical world? Second, can we use these ideas to reconstruct from an explanatory text the physical ideas being communicated? We examine each in turn.

How far can a QP-based frame semantics go in accounting for the semantics of explanatory texts? One way to answer this question is to analyze a corpus of physical explanations, and see what fraction of the sentences require the frames of QP theory (and frames for mental models expressed in QP theory) for their interpretation. We have done this by using four chapters of a book on solar energy, *Sun Up to Sun Down* (Buckley, 1979). We chose this book because it is very clearly written, and we have been using it for a source of examples in other projects, since it uses both diagrams and analogies heavily.³ We chose chapters 2 through 5 because they provide a basic exposition of heat, temperature, and types of heat flow.

Our analysis method was this. Two evaluators familiar with the theory independently scored each sentence. Then

³ As additional corpus material, we have selected a college textbook on the weather as well as a children's book on weather, but while these have served as a source of data for our analysis of syntactic realizations, the results in this section are based only on the Buckley text.

they compared their results, discussing divergences until they came to agreement.

We looked at the linguistic realizations of physical processes in the text. Based on the QP frame semantics, we defined nine types of information about processes: the process name (P), information about subclasses of a process (i.e. a specialization) (SC), participants (PA), about conditions: antecedent activations (AA), antecedent ordinal relations (AO), antecedent relations (AR), and finally about consequences: indirect influences (CII), direct influences (CDI), and consequence relations other than influences (CR).⁴ Multiple pieces of information can appear within a single sentence, so we scored number of phrases of particular types in addition to the number of sentences that they occurred in. Sentences can contain multiple types of information, so the same sentence can appear in multiple categories. We also distinguished between information from examples (identified through a preliminary analysis) and general information, since we have hypothesized (Forbus & Gentner, 1997) that common sense physics arises within-domain analogies involving descriptions. Tables 1 (general information) and 2 (exemplar-specific information) show our results.

Type	P	SC	PA	AA	AO	AR	CR	CDI	CII
#Sentences	10	1	8	15	5	1	9	8	15
#Phrases	11	4	14	16	5	1	18	16	18

Table 1: General statements using QP theory concepts

Type	P	SC	PA	AA	AO	AR	CR	CDI	CII
#Sentences	26	0	28	15	6	5	26	19	14
#Phrases	26	0	74	15	7	5	53	38	17

Table 2: Use of QP theory concepts in examples.

The data shows that the exemplar-specific data contains more than twice the number of processes, about five times the number of participants and a lot more information about the consequences of the mentioned processes. However, the amount of information about the conditions of a process (categories AA, AO, and AR) is nearly the same. As expected, any information about specialization of processes (SC) is only found in the general information.

What kind of coverage does QP theory provide? Of the 216 sentences, 94 of them mention at least one element from the QP frame system proposed here. That means that QP theory can account for roughly 43% of these chapters.

Let us turn to the second question, the reconstruction of a QP domain theory from the frame semantics that one might get from analyzing a text. Again we rely on Chapters 2 through 5 of Buckley (1979). These chapters yield six physical processes: General models of heat flow and volume

flow (e.g., liquid flow), and four subclasses of heat flow (conduction, convection, radiation, and transport). Using this data and the information about the constituents of processes it contains, we attempted to manually reconstruct the models of the underlying physical processes. Figure 1 shows the reconstructed model of the generic heat flow process. One piece of information in Figure 1 marked with a star was not part of any general description of the heat flow process but originated from information about specific examples. It was generalized and included into the generic process model. By combining information from specific examples with general information, reasonable QP theory process descriptions of each were obtained.

These results are very encouraging. The frame semantics based on QP theory provides significant coverage of this corpus. The aspects that are not related to QP theory are not themselves physical laws or behaviors per se, but require frames of the types that would be found in other kinds of texts. Thus these results suggest that the frame semantics we propose using QP theory could play a useful role in a broad system of natural language semantics.

Discussion

This paper argues that qualitative physics, specifically QP theory, can be used as a component in a system of natural language semantics. We outlined how QP theory can be recast in terms of Fillmore's frame semantics, as used in the FrameNet project. The constructs of QP theory can be recast in terms of a collection of frames and subframes, which can be used to describe many causal mental models found in explanatory texts. As the syntactic realizations of these frames are further worked out, we believe that they will be a valuable extension to FrameNet semantics.

In addition to broadening the coverage of FrameNet to include a wide range of continuous phenomena and systems, our extension also grounds these new frames in terms of a well-worked out knowledge representation formalism capable of supporting qualitative reasoning. The compatibility of existing FrameNet motion descriptions with this model, and our analysis of a QP model of flow in frame semantics, lends support to our claim that this recasting of qualitative modeling can productively extend frame semantics for natural language.

The corpus analysis presented suggests that this extension can be useful, since 43% of the material in sample chapters from a typical science book can be captured in terms of them. Moreover, our analysis suggests that these frames could be composed to construct domain theories of a kind already used in qualitative reasoning.

Our results suggest that QP frame semantics can indeed play an important role in natural language semantics for physical texts. More investigation is needed on several questions, including:

• We want to refine our estimates of coverage by analyzing a larger corpus with a broader range of materials. These analyses are impractical by hand, so we are exploring the use of automated tools for subsequent analyses.

⁴ Although the information involved in these categories has varying complexity, e.g., influences and ordinal relations are more complex than the process or participant names, we do not impose any ordering or weighting on these pieces of information.

```
Process HeatFlow
:participants
loc1 ;; FlowSource
loc2 ;; FlowDest
path ;; FlowPath
:conditions
(> (temp loc1) (temp loc2))
*(heat-aligned path)
:consequences
(from-location loc1)
(to-location loc2)
(qprop- flowrate thermal-resistance)
(I- (heat loc1) flowrate)
(I+ (heat loc2) flowrate)
```

Figure 1: One QP physical process description reconstructed from the Buckley text. The line marked with "*" was derived via generalization from specific examples.

- We view our work as complementary to that of Narayanan (1999), who is linking FrameNet semantics with sensory-motor schemata. Both will ultimately be needed, and their interplay will be interesting to explore.
- The same QP analysis used for literal language could be used to improve the productive understanding of many metaphors. For example, the FrameNet analysis of heat in the emotional domain has tied to it the lemma **boil** directly. If QP representations for heat, heat flow, and boiling were used instead, one could infer that making someone angry for longer could lead to boiling, and that if someone had "boiled over", starting a heat flow with them as the source, could "cool them off".
- A fascinating set of questions arises from cross-linguistic comparisons. Are these ideas bundled up in the same way in all languages, or are they realized very differently (e.g., Bowerman's (1996) cross-linguistic analysis of spatial prepositions, Talmy's (1985) cross-linguistic analysis of verb semantics, and Imai and Gentner's (1993) analysis of the mass/count distinction)?

Another goal of our analysis is synthesis, i.e., to create a habitable controlled language that can be used in natural language processing systems that communicate with people about the physical world more fluently. Such software could be invaluable in creating new kinds of intelligent software, such as tutoring systems and monitoring systems.

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